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# Dynamic Intersection Signal Control Optimization (DISCO)

Hong K LO 羅康錦

[cehklo@ust.hk](mailto:cehklo@ust.hk)

Civil Engineering

Hong Kong University of Science and Technology





# Existing Traffic Signal Control Approaches

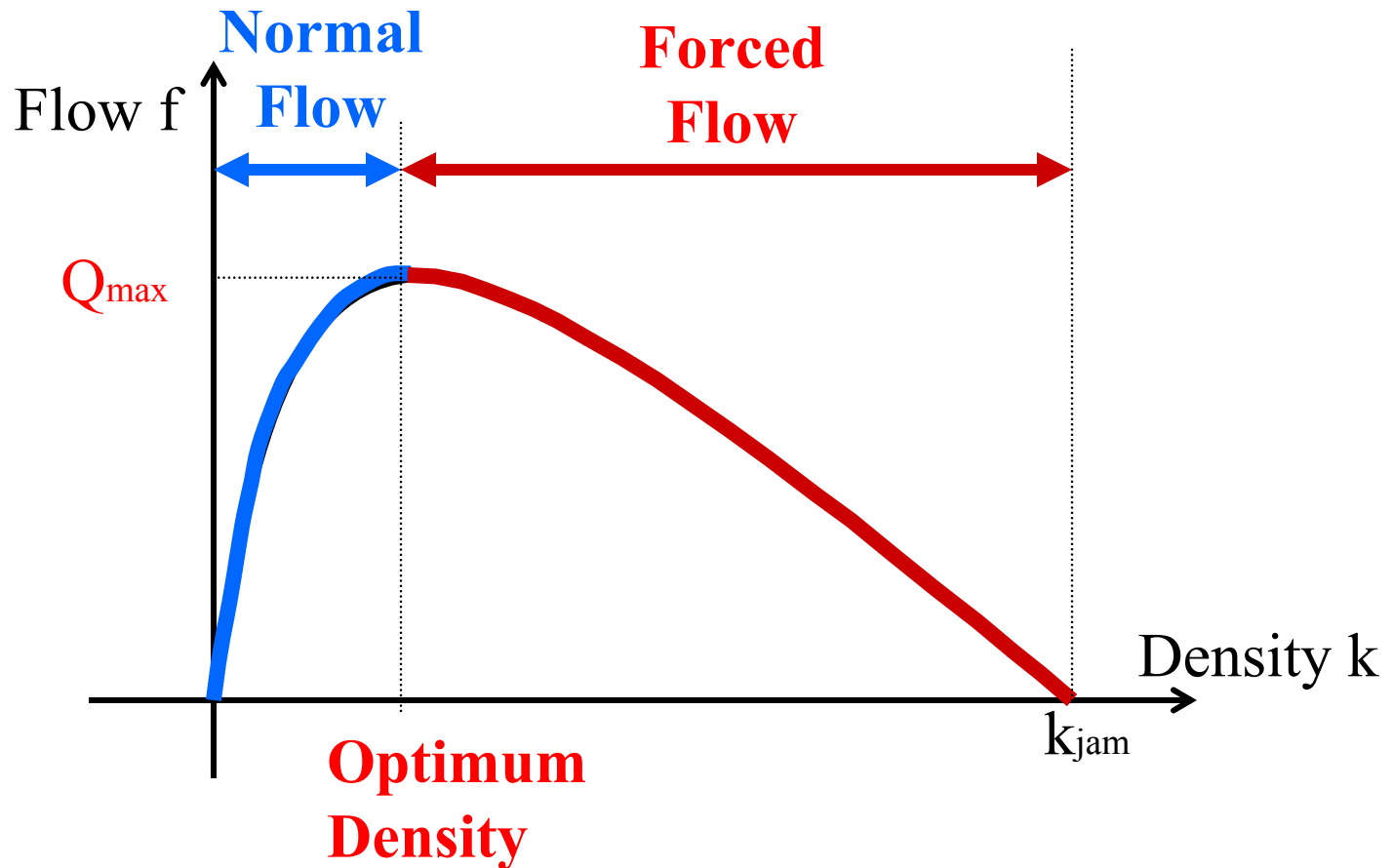
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- Static Models
  - don't work well for congested traffic
  - e.g. TRANSYT, MAXBAND, PASSER
- Dynamic Models
  - don't work for light traffic
  - ignore the fundamental diagram



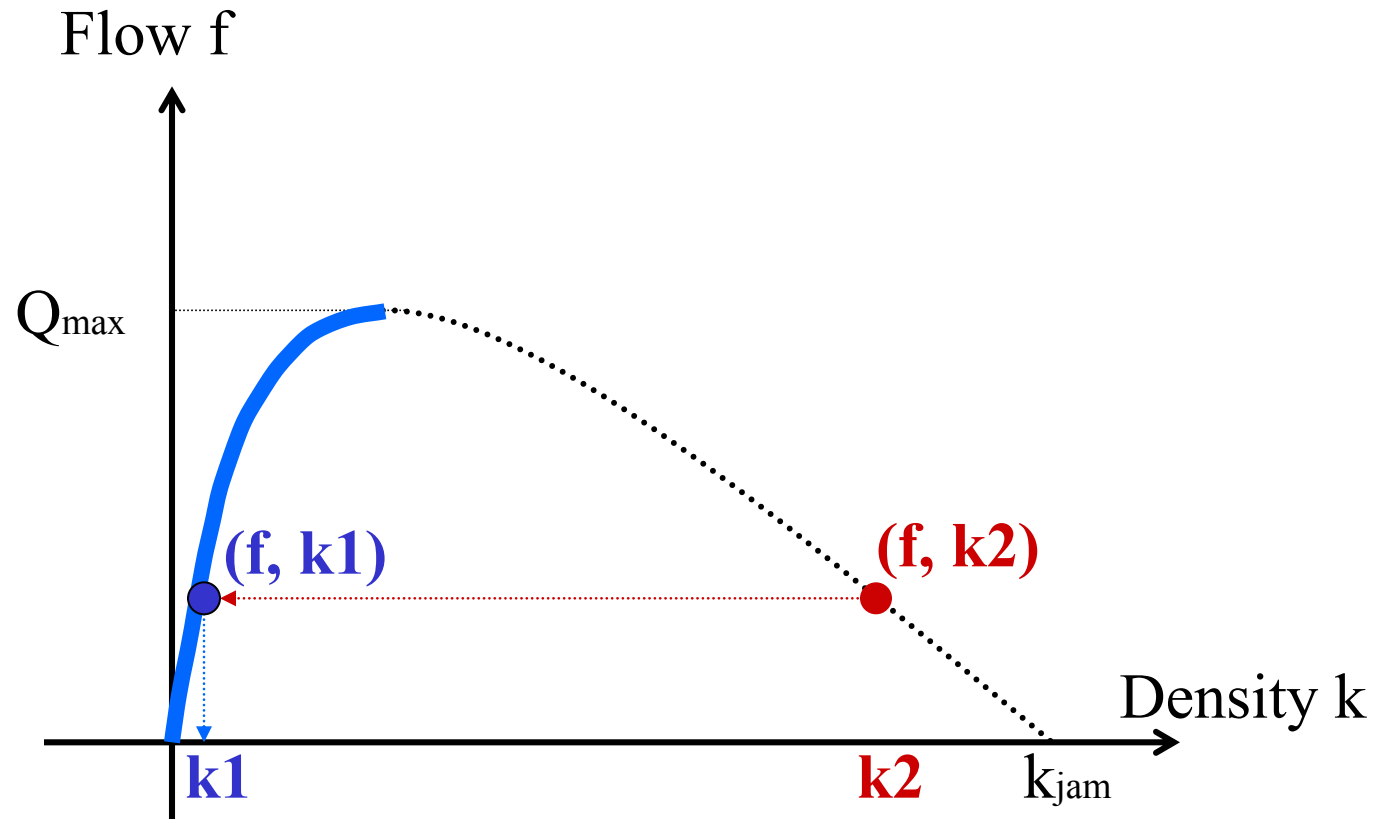


# Fundamental Diagram





# Flow-density Relationship





# Potential Problems

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- No operational model for over-saturated traffic
- Traffic conditions fluctuate from light to saturated daily
- Frequent manual overrides are common





# Features of This New Formulation

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- Models dynamic traffic
- Captures queue dissipation and formation dynamics, kinematic waves.
- Covers the entire range of traffic conditions
- Modify traffic density to the optimum flow level in over-saturated traffic





# Dynamic Intersection Signal Control Optimization (DISCO)

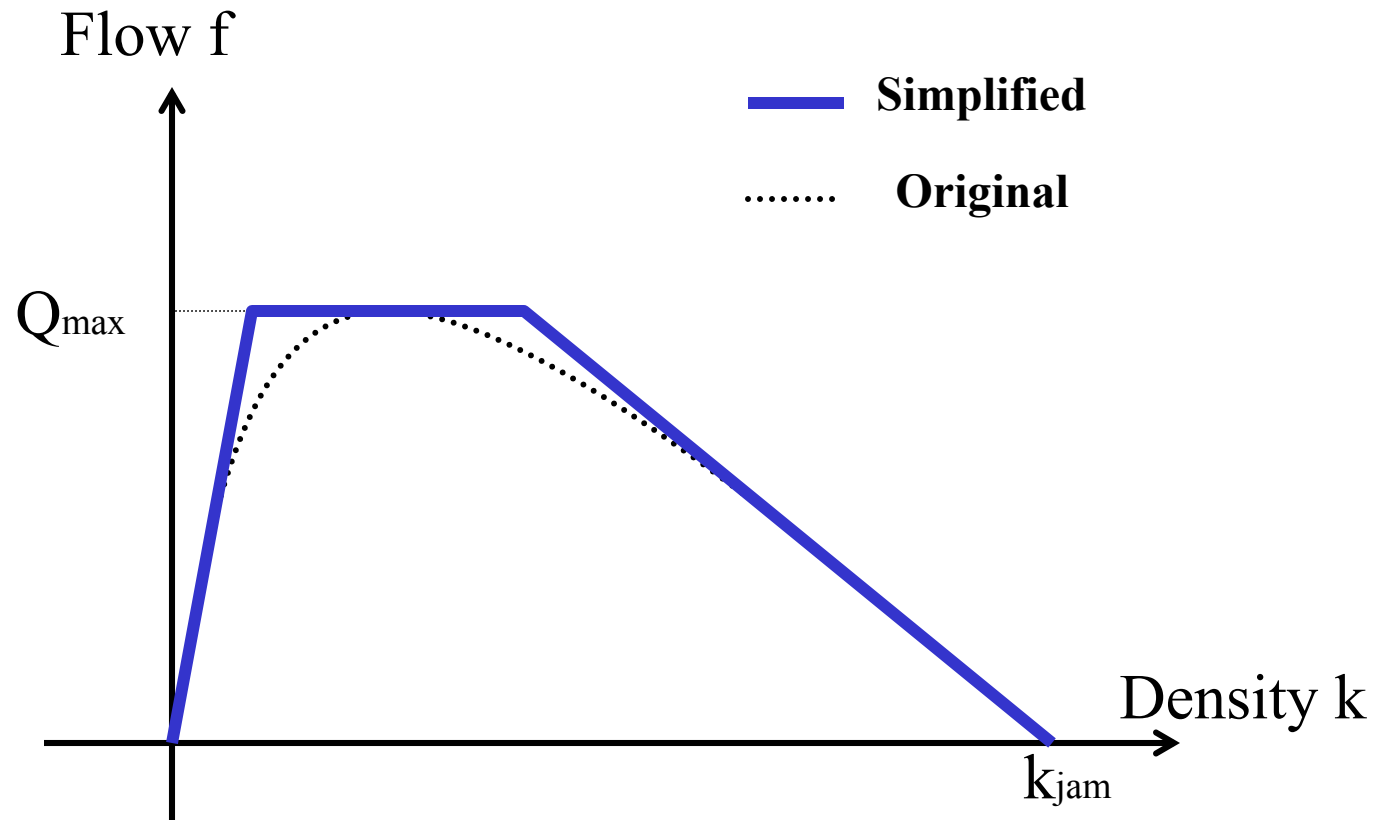
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- Minimize total dynamic delay, subject to
  - Cell-Transmission Model (Daganzo, 1994, 1995) (CTM) to model traffic dynamics
  - Timing plan constraints, max green, cycle time, etc.





# Simplified Flow-density Relationship







# Model Components

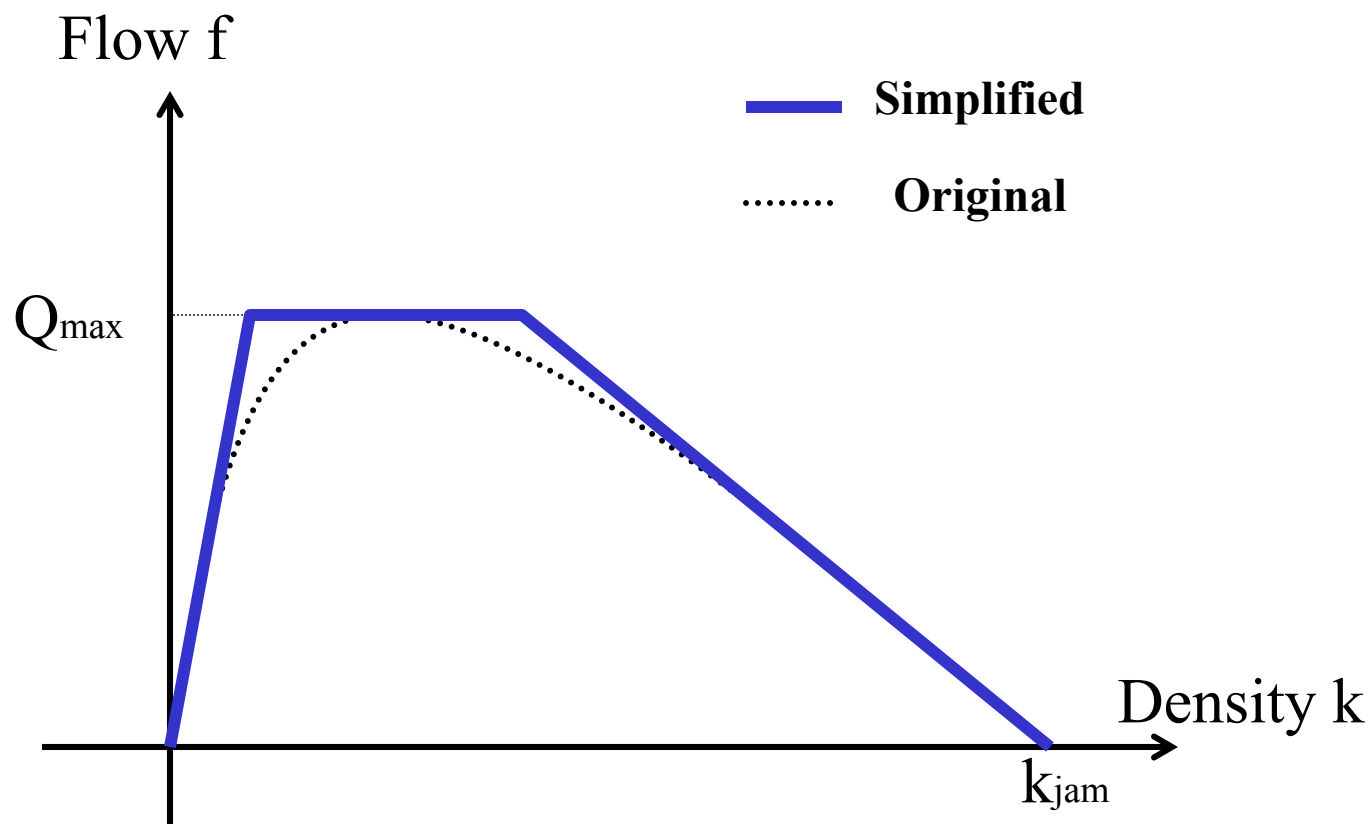
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- Cell-Transmission Model (Daganzo, 1994, 1995) (CTM) to model traffic dynamics
  - a convergent approximation to the Lighthill and Whitham (1955) and Richards (1956) (LWR) model
- Mixed-integer programming technique to incorporate CTM into a mathematical program



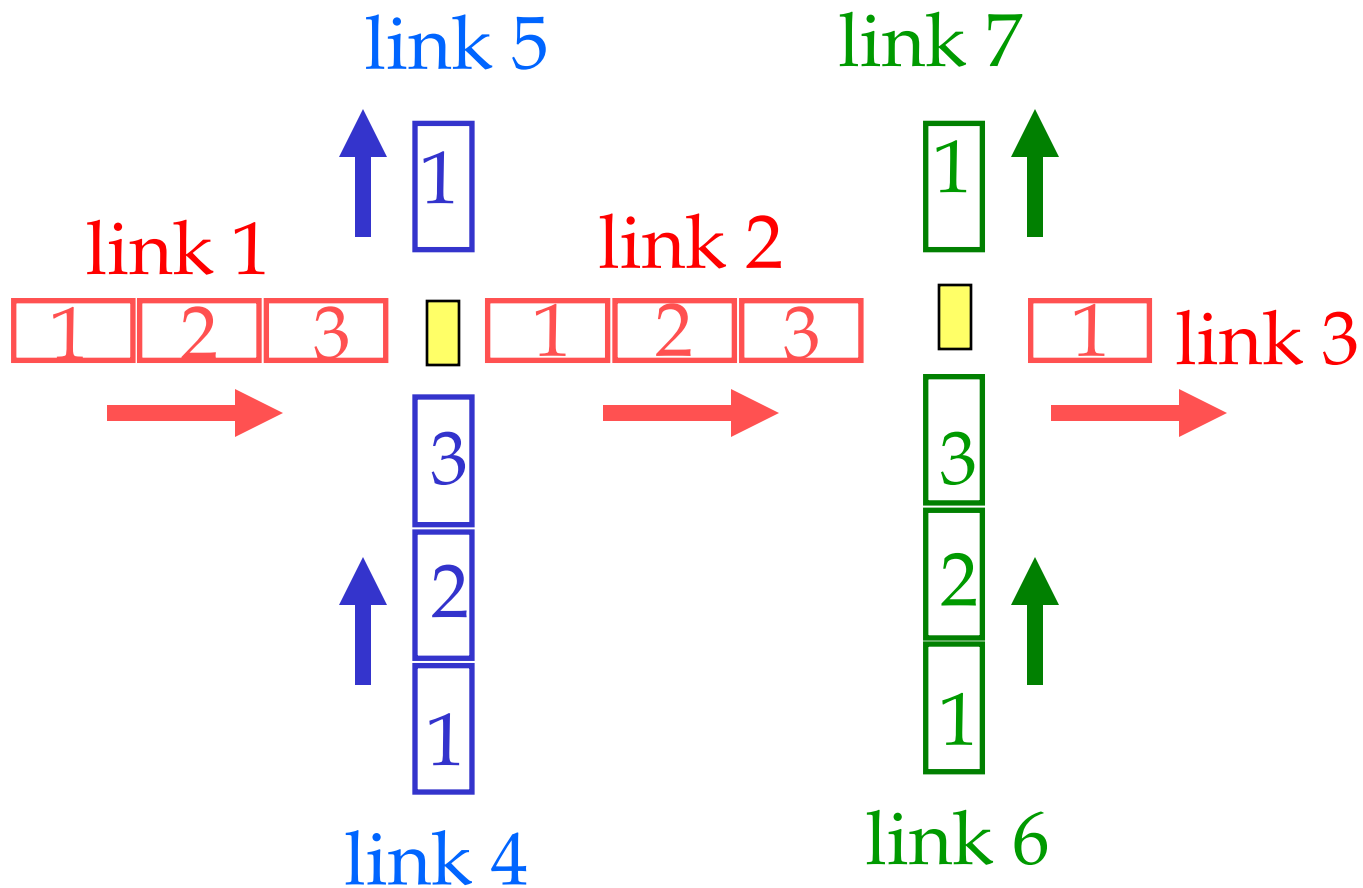


# Simplified Flow-density Relationship





# Network Example





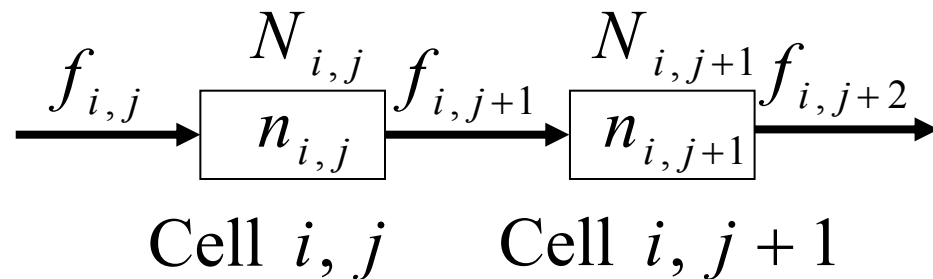
# Cell-Transmission Model: Basic conditions

- Cell inflow equation:

$$f_{i,j+1}(t) = \min \left\{ \underbrace{Q_{i,j+1}(t)}_{\text{Inflow Capacity}}, \underbrace{n_{i,j}(t)}_{\text{Flow waiting}}, \underbrace{\frac{W}{V} [N_{i,j+1}(t) - n_{i,j+1}(t)]}_{\text{Available space}} \right\}$$

- Conservation condition for normal cell:

$$n_{i,j}(t+1) = n_{i,j}(t) + f_{ij}(t) - f_{i,j+1}(t)$$





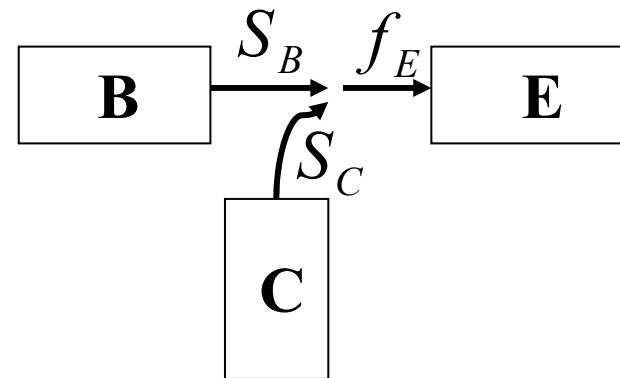
# Cell-Transmission Model: Merges

- Conservation condition for merges:

$$S_C(t) = \min\{n_C(t), Q_C(t), \delta[N_E(t) - n_E(t)]\}$$

$$S_B(t) = \min\{n_B(t), Q_B(t), \delta[N_E(t) - n_E(t)]\}$$

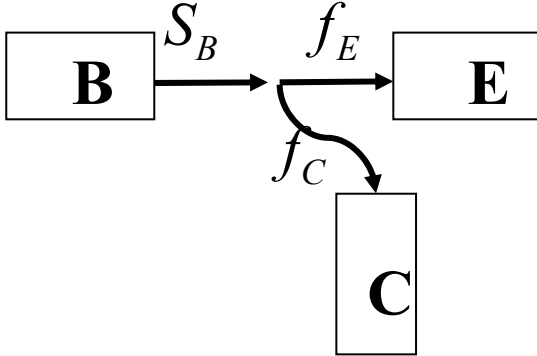
$$f_E(t) = S_C(t) + S_B(t)$$





# Cell-Transmission Model: Diverges

- Conservation condition for diverges:

$$S_B(t) = \min \left\{ \begin{array}{l} n_B(t) \\ Q_B(t) \\ \min \{ Q_E(t), \delta [N_E(t) - n_E(t)] / \beta_E \} \\ \min \{ Q_C(t), \delta [N_C(t) - n_C(t)] / \beta_C \} \end{array} \right\}$$


$$f_C(t) = \beta_C \cdot S_B(t)$$

$$f_E(t) = \beta_E \cdot S_B(t)$$





# Signal Control Formulation (1)

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- Objective function: minimize delay

$$J = \min_{g, r} \sum_t \sum_{i \in E} \sum_j n_{ij}(t) - f_{ij}(t)$$

- Dynamic Demand:

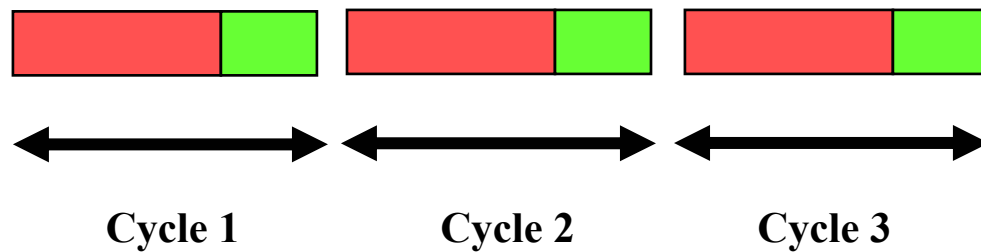
$$Q_{i2}(t) = D_i(t) \quad i \in \Omega$$



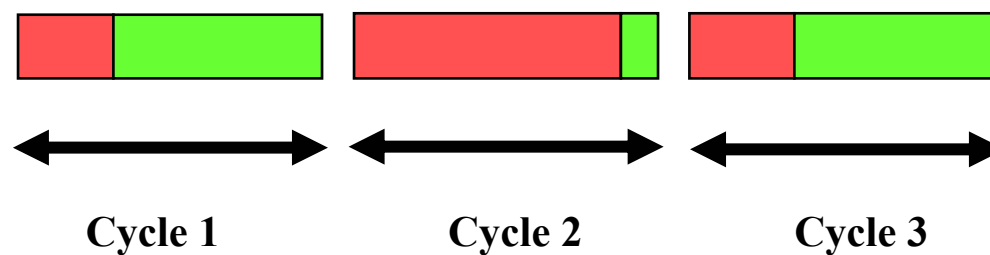


# Signal control methods

**Fixed Green  
Fixed Cycle (FGFC)**



**Variable Green  
Fixed Cycle (VGFC)**



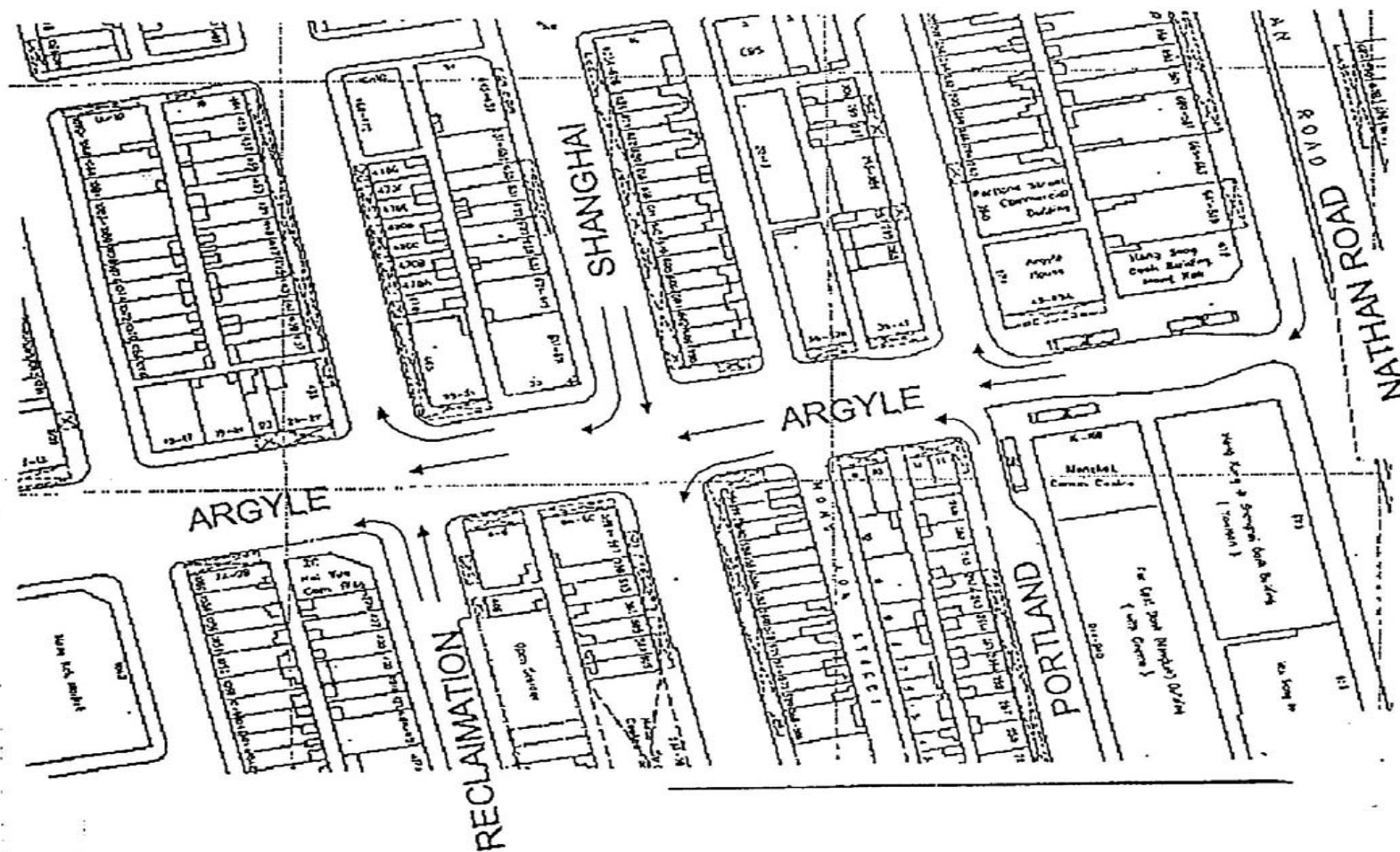
**Variable Green  
Variable Cycle (VGVC)**





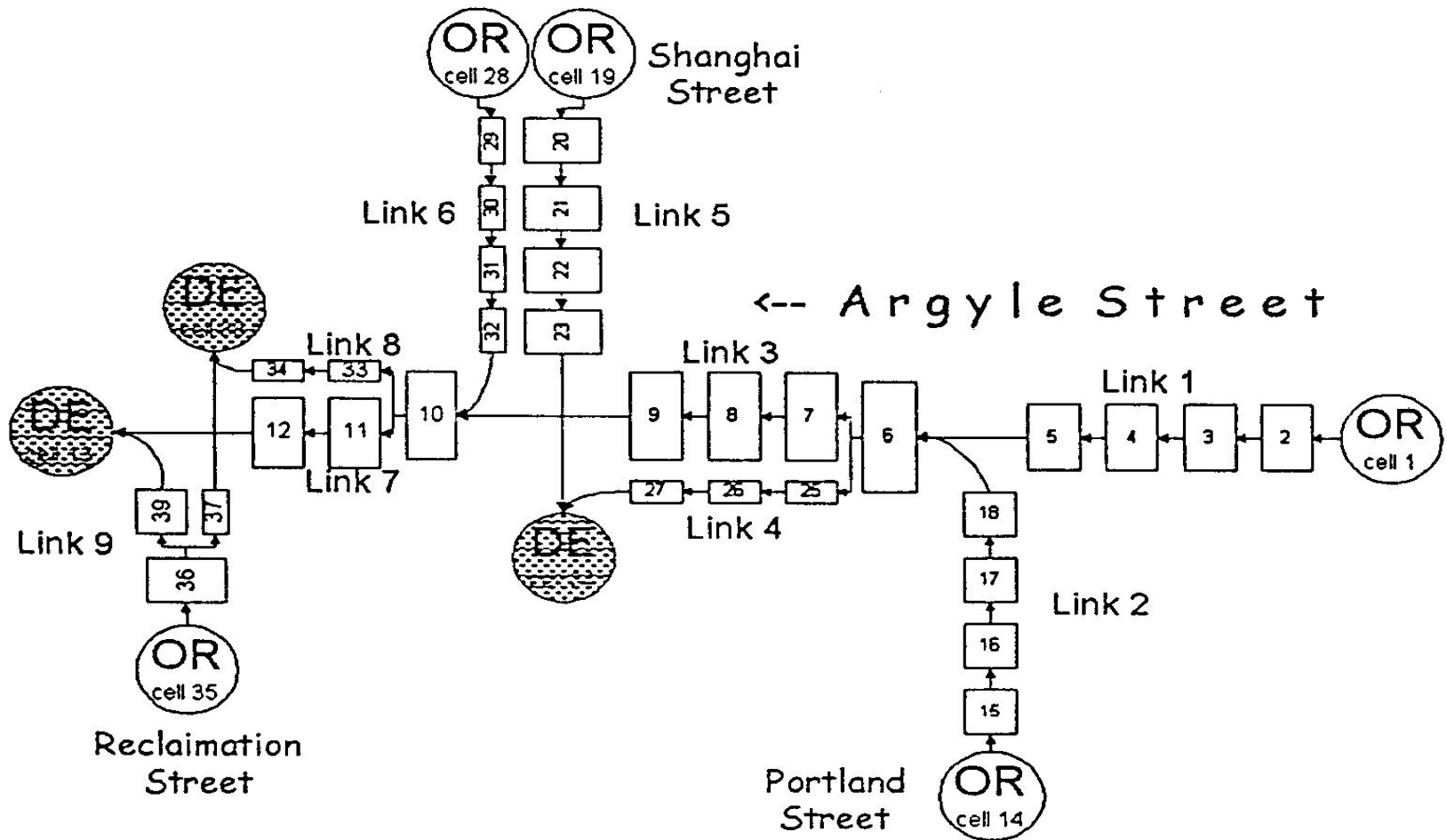


# Test Site: Mong Kok





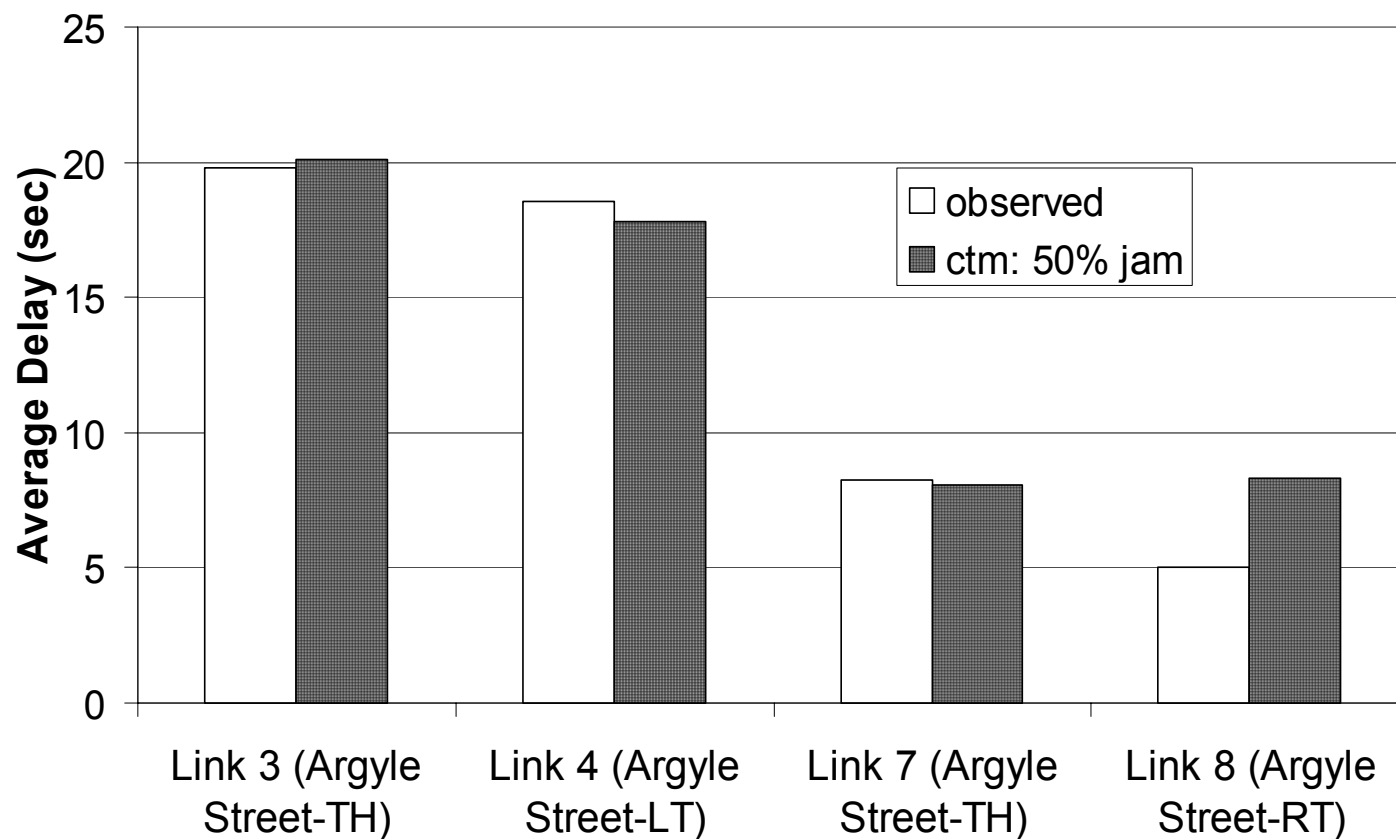
# Model Construction





# Model Validation

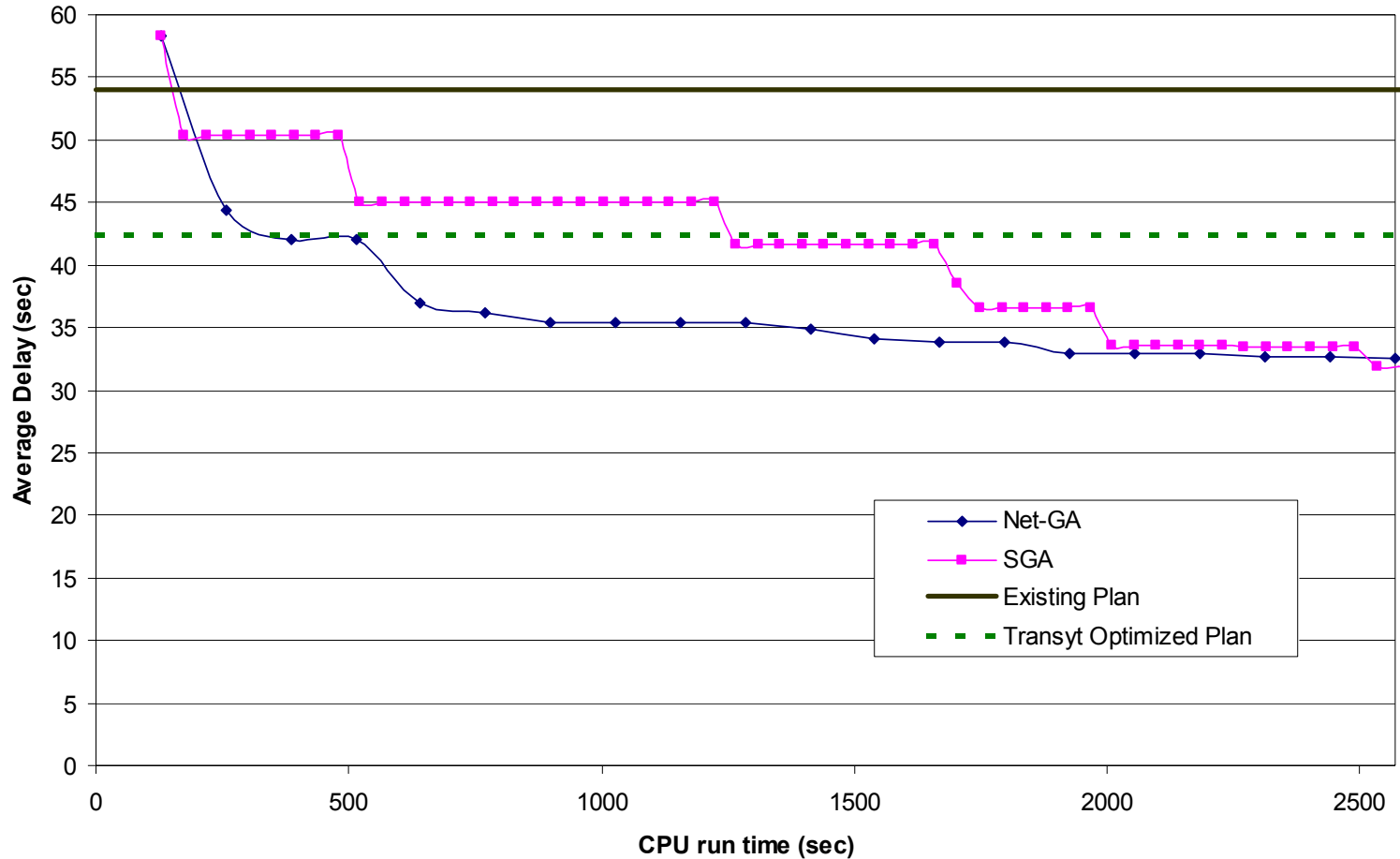
## Delay on Intermediate Links





# Results: Uncongested Case

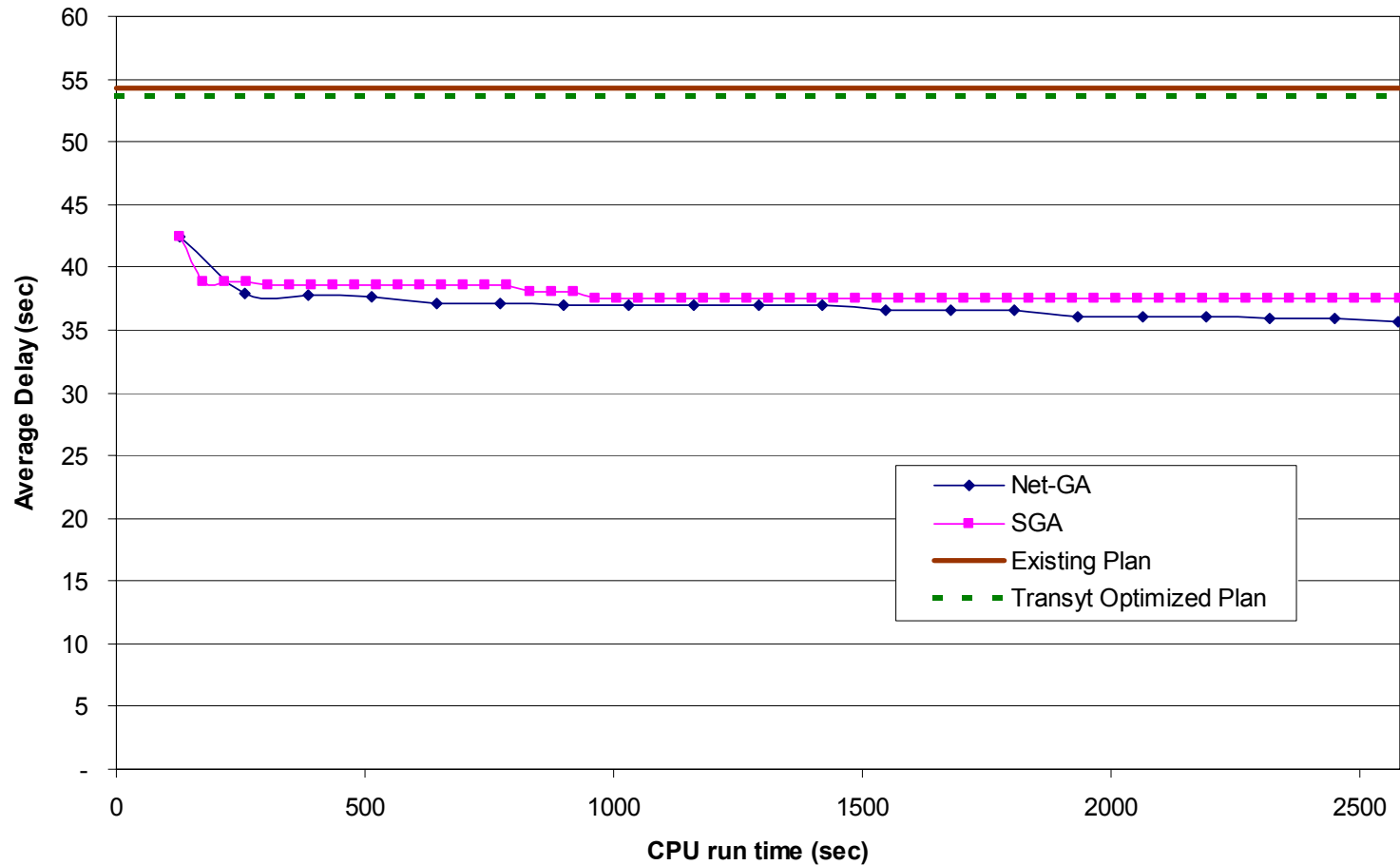
Figure 5-6: Average Delay  
Uncongested Flow, 50% initial cell occupancy (unc50)





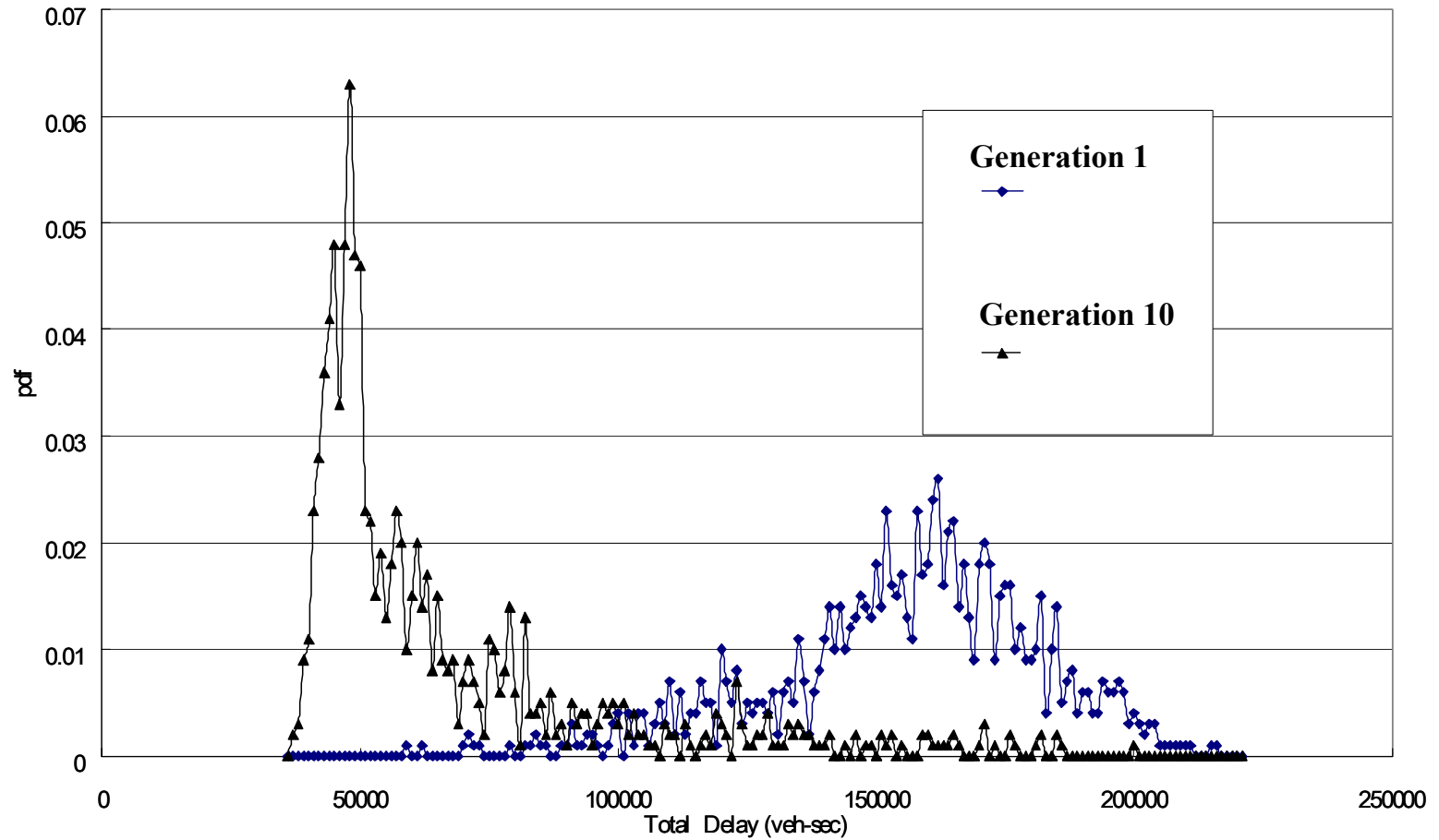
# Results: Congested Case

Figure 5-3: Average Delay  
Congested Flow, 100% initial cell occupancy (con100)





# Performance of Genetic Algorithm





# Results

Delay (veh-hr)	Existing	FGFC	VGFC	VGVC
Fixed Demand	12.0	7.5	7.4	7.4
Time-variant Demand	14.9	10.1	10.0	10.0
Halfly-preloaded	19.5	11.5	11.3	10.9
Fully-preloaded	50.5	34.6	34.3	33.8

% change	Existing	FGFC	VGFC	VGVC
Fixed Demand	0.0	37%	38%	38%
Time-variant Demand	0.0	32%	33%	33%
Halfly-preloaded	0.0	41%	42%	44%
Fully-preloaded	0.0	32%	32%	33%





# Conclusions

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- DISCO works for all traffic conditions
- DISCO has superb performance for congested traffic
- DISCO shows promise as a future dynamic traffic control system

